

Unit VII. Simplifying Rational Expressions Part 1

[31.1]

1.
$$\frac{x(x-2)(x+3)}{x^2(x+3)}$$

1.
$$\frac{x(x+5)(x-8)}{x^3(x+5)}$$

1.
$$\frac{x(x-2)(x+1)}{x^4(x+1)(x-1)}$$

2.
$$\frac{x^3(x-2)^3(x+3)^4}{x^2(x+3)^2}$$

2.
$$\frac{x^4(x+5)^2(x-8)}{x^3(x+5)^3}$$

2.
$$\frac{x^2(x-2)^2(x+1)^3}{x^4(x+1)(x-2)^3}$$

3.
$$\frac{9x^2(x+5)^4(x-5)^4}{6x^2(x-5)^3(x+5)^5}$$

3.
$$\frac{10x(x+1)^4(x-1)^2}{15x(x-1)^3(x+1)^3}$$

3.
$$\frac{20x^3(x+3)^3(x-3)^1}{12x^3(x-3)^2(x+3)^2}$$

Simplifying Rational Expressions Part 1

[31.2]

4.
$$\frac{(x^2 - 9)(x + 4)}{(x + 3)(x^2 - 16)}$$

4.
$$\frac{(x^2 - 25)(x + 6)}{(x + 5)(x^2 - 36)}$$

4.
$$\frac{(x^2 - 49)(x - 8)}{(x - 7)(x^2 - 64)}$$

5.
$$\frac{(4x^2 - 1)(x + 3)}{(2x + 1)(x^2 - 9)}$$

5.
$$\frac{(25x^2 - 16)(x + 7)}{(5x + 4)(x^2 - 49)}$$

5.
$$\frac{(9x^2 - 4)(x - 9)}{(3x - 2)(x^2 - 81)}$$

6.
$$\frac{(4x^2 - 1)(x + 3)^2}{(2x + 1)(x^2 - 9)}$$

6.
$$\frac{(25x^2 - 16)(x + 7)^2}{(5x + 4)(x^2 - 49)}$$

6.
$$\frac{(25x^2 - 4)(x - 1)^2}{(5x - 2)^2(x^2 - 1)}$$

Simplifying Rational Expressions Part 2

[32.1]

1. $\frac{x^2+3x+2}{x^2+4x+3}$

1. $\frac{x^2+4x+3}{x^2+5x+4}$

1. $\frac{x^2+5x+4}{x^2+7x+6}$

2. $\frac{x^2+3x-4}{x^2+2x-3}$

2. $\frac{x^2-3x-10}{x^2-5x-14}$

2. $\frac{x^2+2x-15}{x^2-2x-3}$

3. $\frac{x^2-3x+2}{x^2-1x-2}$

3. $\frac{x^2-1x-6}{x^2-5x+6}$

3. $\frac{x^2-5x+4}{x^2+3x-4}$

Simplifying Rational Expressions Part 2

[32.2]

4. $\frac{2x^2+3x+1}{2x^2+5x+3}$

4. $\frac{3x^2+7x+2}{3x^2+4x-4}$

4. $\frac{3x^2-1x-2}{5x^2-2x-3}$

5. $\frac{x^2-5x-14}{x^2-3x-10}$

5. $\frac{x^2-2x-3}{x^2+2x-15}$

5. $\frac{x^2+3x-4}{x^2+2x-3}$

6. $\frac{x^2-3x+2}{x^2-1}$

6. $\frac{x^2-5x+4}{x^2-16}$

6. $\frac{x^2-4}{x^2-9}$

Adding Rational Expressions

[33.1]

$$1. \quad \frac{4}{x^4(x+3)^2} + \frac{1}{x^2(x+3)^4}$$

$$2. \quad \frac{3}{x(x-5)^3} + \frac{2}{x^3(x-5)^1}$$

$$3. \quad \frac{2}{x(x+2)^3} + \frac{1}{x^4(x+2)^5}$$

$$1. \quad \frac{4}{x^2(x+1)^5} + \frac{1}{x^4(x+1)^3}$$

$$2. \quad \frac{2}{x(x-6)^6} + \frac{3}{x^3(x-6)^4}$$

$$3. \quad \frac{3}{x(x+3)^2} + \frac{1}{x^3(x+3)^4}$$

$$1. \quad \frac{4}{x^3(x+4)^1} + \frac{1}{x^2(x+4)^3}$$

$$2. \quad \frac{2}{x^4(x-4)^2} + \frac{2}{x^1(x-4)^4}$$

$$3. \quad \frac{2}{x^3(x+4)^4} + \frac{2}{x^2(x+4)^6}$$

Adding Rational Expressions

[33.2]

4. $\frac{4}{x^4(x+3)^2} + \frac{1}{x^2(x+3)^3}$

4. $\frac{4}{x^1(x+1)^4} + \frac{1}{x^3(x+1)^3}$

5. $\frac{3}{x(x-5)^5} + \frac{2}{x^3(x-5)^6}$

5. $\frac{2}{x^4(x-6)^5} + \frac{3}{x(x-6)^4}$

6. $\frac{2}{x(x+2)^4} + \frac{1}{x^4(x+2)^3}$

6. $\frac{3}{x(x+3)^5} + \frac{1}{x^5(x+3)^4}$

4. $\frac{4}{x^3(x+4)^1} + \frac{1}{x^2(x+4)^2}$

5. $\frac{2}{x^3(x-4)^1} + \frac{2}{x^2(x-4)^2}$

6. $\frac{2}{x^3(x+4)^2} + \frac{2}{x(x+4)^1}$

Adding Rational Expressions

[33.3]

7. $\frac{5}{3x^4(x+3)^7} + \frac{3}{2x^2(x+3)^6}$

7. $\frac{3}{4x^2(x+1)^6} + \frac{1}{3x^4(x+1)^5}$

7. $\frac{7}{5x^3(x+4)^2} + \frac{3}{4x^2(x+4)^1}$

8. $\frac{4}{5x^2(x-7)^3} + \frac{1}{6x^3(x-7)^2}$

8. $\frac{3}{4x^5(x-5)^4} + \frac{1}{3x^3(x-5)^3}$

8. $\frac{1}{2x^1(x-4)^2} + \frac{2}{3x^3(x-4)^1}$

9. $\frac{4}{3x^5(x-2)^2} + \frac{2}{6x^3(x-2)^1}$

9. $\frac{5}{2x^6(x-1)^4} + \frac{3}{4x^3(x-1)^3}$

9. $\frac{3}{2x^1(x-5)^5} + \frac{5}{6x^3(x-5)^4}$

Adding Rational Expressions

[33.4]

10. $\frac{5}{6x^4(x-1)^6} + \frac{3}{4x^3(x-1)^5}$

10. $\frac{4}{8x^4(x-5)^4} + \frac{2}{6x^5(x-5)^3}$

11. $\frac{3}{6x^4(x-4)^1} + \frac{4}{3x^6(x-4)^2}$

11. $\frac{4}{4x^5(x-6)^3} + \frac{3}{2x^3(x-6)^4}$

12. $\frac{4}{12x^3(x+1)^1} + \frac{2}{8x^3(x+1)^2}$

12. $\frac{5}{12x^4(x+1)^3} + \frac{3}{9x^4(x+1)^4}$

10. $\frac{7}{9x^3(x-7)^2} + \frac{2}{6x^2(x-7)^1}$

11. $\frac{3}{4x^1(x-8)^5} + \frac{2}{8x^3(x-8)^6}$

12. $\frac{3}{15x^1(x+7)^4} + \frac{2}{6x^1(x+7)^5}$

Solving rational equations

[34.1]

Solve for x

$$1. \quad \frac{2}{3x} + \frac{1}{2x} = \frac{1}{4}$$

$$1. \quad \frac{1}{2x} + \frac{3}{5x} = \frac{1}{4}$$

$$1. \quad \frac{3}{4x} + \frac{2}{5x} = \frac{1}{2}$$

$$2. \quad \frac{2}{3} + \frac{1}{2} = \frac{1}{4x}$$

$$2. \quad \frac{1}{2} + \frac{3}{5} = \frac{1}{4x}$$

$$2. \quad \frac{3}{4} + \frac{2}{5} = \frac{1}{2x}$$

Solving rational equations

[34.2]

Solve for x

$$3. \quad \frac{2}{9} + \frac{1}{6x} = \frac{2}{3} - \frac{5}{2x}$$

$$3. \quad \frac{1}{2} + \frac{2}{3x} = \frac{1}{12} - \frac{5}{4x}$$

$$3. \quad \frac{4}{9x} - \frac{5}{6x} = \frac{2}{3x} + \frac{1}{6}$$

$$4. \quad \frac{4}{3x} - \frac{1}{6x} = \frac{5}{2} - \frac{1}{3}$$

$$4. \quad \frac{5}{2x} - \frac{2}{4x} = \frac{11}{8} - \frac{1}{2}$$

$$4. \quad \frac{4}{9} - \frac{5}{6} = \frac{2}{3x} - \frac{1}{6x}$$

Solving rational equations

[34.3]

Solve for x

$$5. \quad \frac{3}{8} + \frac{1}{4x} = \frac{3}{2} - \frac{5}{x}$$

$$5. \quad \frac{7}{10} + \frac{2}{5x} = \frac{1}{2} - \frac{5}{x}$$

$$5. \quad \frac{5}{9} + \frac{1}{6x} = \frac{2}{3} - \frac{5}{x}$$

$$6. \quad \frac{5}{3x} - \frac{1}{6x} = \frac{3}{2} - \frac{1}{3}$$

$$6. \quad \frac{3}{2x} - \frac{1}{4x} = \frac{5}{8} - \frac{1}{2}$$

$$6. \quad \frac{4}{9x} - \frac{5}{6x} = \frac{2}{3} - \frac{1}{6}$$

Isolating terms in formulas

[35.1]

Solve for the given term

$$1. \quad A = 4\pi r^2, r$$

$$1. \quad A = 36\pi r^2, r$$

$$1. \quad A = 9\pi r^2, r$$

$$2. \quad A = \frac{a+b+c}{3}, c$$

$$2. \quad A = \frac{a+b}{2}, b$$

$$2. \quad A = \frac{a+b+c+d}{4}, a$$

$$3. \quad A = k(b - c + d), b \quad 3. \quad A = k(b - c), b \quad 3. \quad A = k(b - c + d - e), b$$

Solve for the given term

$$4. \quad A = 5(2b + 3c), b$$

$$4. \quad B = 7(3b + 4c), b$$

$$4. \quad C = 9(4b + 5c), b$$

$$5. \quad A = \frac{h(b_1 - b_2 + b_3)}{3}, b_1$$

$$5. \quad A = \frac{h(b_1 + b_2 - b_3)}{3}, b_1$$

$$5. \quad A = \frac{h(b_1 + b_2)}{2}, b_1$$

Solve for the given term

$$6. \quad a^2 - b^2 + c^2 = d^2, a \quad 6. \quad a^2 - b^2 - c^2 = d^2, a \quad 6. \quad a^2 + b^2 = c^2, a$$

$$7. \quad a^3 - b^3 - c^3 = d, a \quad 7. \quad a^3 - b^3 + c^3 = d, a \quad 7. \quad a^3 + b^3 + c^3 = d, a$$

$$8. \quad \sqrt[3]{a^2 + b^2 + c^2} = d, c \quad 8. \quad \sqrt[4]{a^2 - b^2 + c^2} = d, c \quad 8. \quad \sqrt{c^2 - b^2} = a, c$$